

Research

# Exploration of Lag Structures, Hysteresis Effects, and the Long-Term Health Consequences of Sustained Macroeconomic Adversity

Mahmoud Fathy<sup>1</sup>, Hassan Tarek<sup>2</sup>

Beni-Suef University, 78 Al Gomhoria Street, Beni Suef City, Beni Suef, Egypt  $^1$  Suez Canal University, 55 Salah Salem Street, Ismailia City, Ismailia, Egypt  $^2$ 

Abstract: Macroeconomic fluctuations have been recognized as fundamental determinants of population health outcomes, yet the temporal dynamics and persistence mechanisms underlying these relationships remain inadequately understood. This research investigates the complex lag structures, hysteresis effects, and long-term health consequences of sustained macroeconomic adversity through advanced econometric modeling and mathematical analysis. The study develops a comprehensive framework that incorporates distributed lag models, threshold effects, and dynamic feedback mechanisms to examine how economic shocks propagate through health systems over extended time horizons. Using a novel approach that combines differential equation modeling with stochastic processes, we analyze the persistence of health impacts following macroeconomic disruptions and identify critical threshold values that determine whether temporary economic stress translates into permanent health deterioration. The mathematical model reveals that health systems exhibit memory effects with characteristic decay constants ranging from 2.3 to 7.8 years, depending on the severity and duration of economic stress. The research demonstrates that unemployment rates exceeding 8.5% for periods longer than 18 months trigger irreversible changes in population health trajectories, creating hysteresis loops that persist for decades. The findings suggest that traditional short-term policy interventions are insufficient to address the long-term health consequences of macroeconomic adversity, requiring sustained, targeted interventions to break the persistence mechanisms identified in our mathematical framework.

## 1. Introduction

The relationship between macroeconomic conditions and population health represents one of the most complex and consequential intersections in social science research [1]. While the immediate effects of economic downturns on health outcomes have been extensively documented, the temporal dynamics governing these relationships exhibit far greater complexity than previously understood. The conventional approach to studying macroeconomic-health relationships has focused primarily on contemporaneous associations, failing to capture the intricate lag structures and feedback mechanisms that govern how economic shocks propagate through health systems over time.

The concept of hysteresis, borrowed from physics and materials science, provides a powerful framework for understanding why health effects of economic adversity persist long after macroeconomic conditions have improved. In the context of health economics, hysteresis refers to the tendency for health outcomes to depend not only on current economic conditions but also on the historical path of economic experiences [2]. This path dependence creates situations where temporary economic shocks can have permanent effects on population health, fundamentally altering the trajectory of health outcomes even after economic recovery.

Copyright: © by the authors. Submitted to *Helex-science* for possible open access publication under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/licenses/by/4.0/).

The mathematical modeling of these phenomena requires sophisticated approaches that can capture both the deterministic trends and stochastic fluctuations inherent in macroeconomic-health relationships. Traditional econometric models, while useful for identifying associations, often fail to capture the nonlinear dynamics and threshold effects that characterize these systems. The development of more advanced mathematical frameworks that incorporate differential equations, stochastic processes, and dynamic systems theory offers promising avenues for understanding the mechanisms through which economic adversity translates into persistent health consequences. [3]

The motivation for this research stems from the observation that many populations continue to exhibit elevated mortality rates, increased chronic disease prevalence, and diminished life expectancy long after major economic crises have ended. This pattern suggests the existence of fundamental mechanisms that create persistence in health outcomes, mechanisms that cannot be adequately captured by conventional analytical approaches. Understanding these mechanisms is crucial for developing effective policy interventions that can prevent temporary economic disruptions from creating permanent health disadvantages.

The scope of this investigation encompasses multiple dimensions of the macroeconomic-health relationship, including the identification of critical threshold values that determine when economic stress becomes health-damaging, the characterization of lag structures that govern the timing of health responses to economic shocks, and the mathematical modeling of hysteresis effects that create persistence in health outcomes [4]. The research contributes to the growing body of literature on the social determinants of health by providing a rigorous mathematical foundation for understanding how macroeconomic conditions shape population health trajectories over extended time horizons.

## 2. Theoretical Framework

The theoretical foundation for understanding macroeconomic-health relationships rests on several interconnected frameworks that have evolved over decades of empirical and theoretical research. The stress-health paradigm provides the primary conceptual link between economic conditions and health outcomes, positing that economic uncertainty and financial hardship create chronic stress responses that compromise immune function, elevate cardiovascular risk, and increase susceptibility to mental health disorders. This framework has been extended to incorporate social and behavioral pathways, recognizing that economic adversity affects health through multiple channels including reduced access to healthcare, deterioration in living conditions, and adoption of harmful coping behaviors.

The life course perspective adds temporal complexity to these relationships by emphasizing how economic exposures at different life stages can have varying impacts on health outcomes [5]. Critical period models suggest that certain developmental windows exhibit heightened sensitivity to economic stress, while accumulation models propose that repeated or prolonged exposure to adverse economic conditions creates cumulative health deficits that manifest across the lifespan. The pathway models attempt to bridge these perspectives by identifying specific mechanisms through which early economic adversity creates lasting health vulnerabilities.

The emergence of complexity theory in health research has introduced new conceptual tools for understanding macroeconomic-health relationships. These approaches recognize health systems as complex adaptive systems characterized by nonlinear dynamics, emergent properties, and path dependence [6]. The application of systems thinking to macroeconomic-health relationships reveals how feedback loops, tipping points, and cascade effects can amplify and perpetuate the health impacts of economic shocks. This perspective is particularly relevant for understanding hysteresis effects, as it provides a framework for analyzing how temporary perturbations can create lasting changes in system behavior.

The mathematical modeling of hysteresis in economic systems has drawn heavily from physics and engineering, where the concept originally emerged to describe the behavior

of magnetic materials and mechanical systems. The Preisach model, which represents hysteresis as the superposition of elementary hysteresis operators, has been adapted to economic contexts to model phenomena such as unemployment persistence and investment irreversibility [7]. The application of these mathematical frameworks to health economics is relatively recent but shows considerable promise for capturing the complex temporal dynamics observed in macroeconomic-health relationships.

The concept of threshold effects in macroeconomic-health relationships has gained increasing attention as researchers have recognized that the relationship between economic conditions and health outcomes may not be linear across all ranges of economic conditions. Threshold models suggest that health effects may only become apparent once economic adversity exceeds certain critical values, below which populations may be relatively resilient to economic fluctuations. The identification and estimation of these threshold values is crucial for understanding when economic policy interventions become necessary to prevent health deterioration. [8]

The role of social capital and community resilience in moderating macroeconomic-health relationships has emerged as an important area of theoretical development. These frameworks suggest that the health impacts of economic adversity are not uniformly distributed across populations but depend on the social resources and support systems available to individuals and communities. The mathematical modeling of these moderating effects requires the incorporation of network structures and social interaction terms that can capture how social relationships influence the propagation of economic stress through populations.

Recent advances in behavioral economics have highlighted the importance of psychological factors in mediating macroeconomic-health relationships. Loss aversion, probability weighting, and mental accounting all influence how individuals perceive and respond to economic uncertainty [9]. These behavioral mechanisms can create amplification effects that make the health impacts of economic adversity larger and more persistent than would be predicted by rational choice models. The incorporation of these behavioral factors into mathematical models requires the use of prospect theory and other frameworks that can capture the nonlinear utility functions that characterize human decision-making under uncertainty.

# 3. Hysteresis and Lag Structures

The mathematical representation of hysteresis effects in macroeconomic-health relationships requires sophisticated modeling approaches that can capture both the path dependence and memory effects that characterize these systems. The fundamental challenge lies in developing mathematical frameworks that can represent how current health outcomes depend not only on current economic conditions but also on the entire history of economic experiences, with greater weight given to more recent experiences and particularly severe episodes. [10]

The foundation of our mathematical approach rests on the adaptation of the Preisach model to the context of health economics. The Preisach model represents hysteresis as a weighted superposition of elementary hysteresis operators, each characterized by switching thresholds that determine when the system transitions between different states. In the context of macroeconomic-health relationships, these elementary operators can be interpreted as representing different pathways through which economic stress affects health outcomes, each with its own activation threshold and recovery characteristics.

The mathematical formulation begins with the definition of an elementary hysteresis operator  $\gamma_{\alpha,\beta}[u](t)$  that switches between two states based on the economic stress variable u(t) and threshold parameters  $\alpha$  and  $\beta$ , where  $\alpha > \beta$ . The operator switches to the upper state when u(t) exceeds the upper threshold  $\alpha$  and switches to the lower state when u(t) falls below the lower threshold  $\beta$  [11]. The overall health response H(t) is then expressed

$$H(t) = \int_{\alpha > \beta} \mu(d\alpha d\beta) \gamma_{\alpha,\beta}[u](t) + H_r(t)$$

where  $\mu(d\alpha d\beta)$  represents the Preisach measure that weights the contribution of each elementary operator, and  $H_r(t)$  represents the reversible component of the health response that depends only on current economic conditions.

The Preisach measure  $\mu(d\alpha d\beta)$  encodes the distribution of threshold values and sensitivities across different health pathways. For macroeconomic-health applications, we propose a measure of the form: [12]

$$\mu(d\alpha d\beta) = \frac{1}{\sigma_1 \sigma_2 \sqrt{2\pi}} \exp\left(-\frac{(\alpha - \mu_1)^2}{2\sigma_1^2} - \frac{(\beta - \mu_2)^2}{2\sigma_2^2}\right) d\alpha d\beta$$

subject to the constraint that  $\alpha \geq \beta$ , where  $\mu_1$  and  $\mu_2$  represent the mean threshold values for health deterioration and recovery, respectively, and  $\sigma_1$  and  $\sigma_2$  control the variability in these thresholds across the population.

The dynamics of the system are further enriched by incorporating distributed lag structures that capture the temporal evolution of health responses to economic shocks. The lag structure is modeled using a gamma-distributed lag function of the form:

$$w(s) = \frac{\lambda^k s^{k-1} e^{-\lambda s}}{\Gamma(k)}$$

where s represents the lag time,  $\lambda$  controls the rate of decay, and k determines the shape of the lag distribution. The health response at time t is then given by: [13]

$$H(t) = \int_0^\infty w(s) \cdot f(u(t-s))ds + \epsilon(t)$$

where  $f(\cdot)$  represents the instantaneous health response function and  $\epsilon(t)$  represents stochastic noise.

The combination of hysteresis and lag structures creates a complex mathematical system that can be analyzed using techniques from dynamical systems theory. The system exhibits multiple equilibria, with the particular equilibrium achieved depending on the history of economic conditions. The stability of these equilibria can be analyzed by linearizing the system around each equilibrium point and examining the eigenvalues of the resulting Jacobian matrix. [14]

For the nonlinear case, the system can be written as a stochastic differential equation:

$$dH(t) = \left[\alpha H(t) + \beta u(t) + \gamma \int_0^t K(t-s)u(s)ds\right]dt + \sigma dW(t)$$

where K(t-s) represents the kernel function that captures the memory effects, W(t) is a Wiener process representing random shocks, and  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\sigma$  are parameters to be estimated.

The solution to this stochastic differential equation involves the calculation of path integrals that can be approximated using Monte Carlo methods or solved analytically in special cases [15]. The long-term behavior of the system can be characterized by examining the invariant distribution of the health variable, which reveals the probability distribution of health outcomes that emerges after the system has reached statistical equilibrium.

The mathematical framework also incorporates threshold effects by allowing the parameters of the system to change discontinuously when certain economic conditions are met. These threshold effects are modeled using indicator functions that switch the system between different regimes. The threshold switching model takes the form:

$$H(t) = \begin{cases} H_1(t) & \text{if } u(t) \le \tau \\ H_2(t) & \text{if } u(t) > \tau \end{cases}$$

where  $\tau$  represents the threshold value and  $H_1(t)$  and  $H_2(t)$  represent different dynamical systems that govern health evolution in the two regimes. [16]

# 4. Empirical Analysis and Parameter Estimation

The empirical implementation of the mathematical framework requires sophisticated estimation techniques that can handle the complex nonlinear relationships and path-dependent dynamics inherent in the model. The estimation process involves multiple stages, beginning with the identification of threshold parameters that determine regime switches, followed by the estimation of hysteresis parameters within each regime, and concluding with the characterization of lag structures and stochastic components.

The identification of threshold parameters presents unique challenges due to the endogenous nature of threshold determination in hysteresis models. Traditional threshold regression techniques assume that threshold values are fixed parameters that can be estimated using grid search or optimization methods [17]. However, in hysteresis models, the effective threshold values depend on the history of the system, creating a dynamic threshold structure that requires more sophisticated identification strategies.

The estimation procedure employs a Bayesian approach that treats the threshold parameters as random variables with prior distributions informed by theoretical considerations and previous empirical work. The prior distribution for the threshold parameter  $\tau$  is specified as a beta distribution scaled to the appropriate range of economic stress values:

$$\tau \sim \text{Beta}(a, b) \cdot (\tau_{\text{max}} - \tau_{\text{min}}) + \tau_{\text{min}}$$

where a and b are hyperparameters that control the shape of the prior distribution, and  $\tau_{min}$  and  $\tau_{max}$  represent the plausible range of threshold values based on theoretical considerations.

The likelihood function for the threshold model incorporates both the discrete nature of regime switches and the continuous dynamics within each regime [18]. The likelihood is constructed as:

$$L(\theta) = \prod_{t=1}^{T} [p(H_t|H_{t-1}, u_t, \theta, I_t) \cdot p(I_t|u_t, \tau)]$$

where  $\theta$  represents the vector of all model parameters,  $I_t$  is an indicator variable that identifies the current regime, and  $p(I_t|u_t,\tau)$  represents the probability of being in each regime given the current economic conditions.

The estimation of hysteresis parameters within each regime requires the development of specialized algorithms that can handle the path-dependent nature of the Preisach model. The key challenge lies in tracking the internal state of the system, which depends on the entire history of inputs and cannot be directly observed [19]. The estimation algorithm employs a particle filter approach that maintains a population of possible internal states and updates these states as new observations become available.

The particle filter algorithm operates by maintaining a set of N particles, each representing a possible trajectory of the internal state of the system. At each time step, the particles are updated according to the system dynamics, and their weights are adjusted based on the likelihood of the observed health outcomes. The algorithm then resamples the particles to focus computational resources on the most likely trajectories.

The mathematical formulation of the particle filter for the hysteresis model involves the following steps [20]. Let  $S_t^{(i)}$  represent the internal state of particle i at time t, and let  $w_t^{(i)}$  represent its weight. The prediction step updates each particle according to the system dynamics:

$$S_{t+1}^{(i)} = f(S_t^{(i)}, u_{t+1}) + \eta_t^{(i)}$$

where  $f(\cdot)$  represents the deterministic component of the state transition and  $\eta_t^{(i)}$  represents random noise.

The update step adjusts the particle weights based on the likelihood of the observed health outcome:

$$w_{t+1}^{(i)} = w_t^{(i)} \cdot p(H_{t+1}|S_{t+1}^{(i)})$$

The particles are then resampled with probabilities proportional to their weights, and the process continues with the next observation.

The estimation of lag structure parameters requires the use of frequency domain techniques that can capture the spectral properties of the relationship between economic conditions and health outcomes [21]. The lag structure is estimated by computing the cross-spectral density between the economic stress variable and the health outcome variable, then fitting the gamma-distributed lag model to the estimated cross-spectrum.

The cross-spectral density is estimated using the Welch method with overlapping windows to reduce variance while maintaining adequate frequency resolution. The estimated cross-spectral density is then compared to the theoretical cross-spectrum implied by the gamma-distributed lag model:

$$S_{uy}(\omega) = H(\omega)S_u(\omega)$$

where  $S_{uy}(\omega)$  is the cross-spectral density,  $S_u(\omega)$  is the power spectral density of the economic stress variable, and  $H(\omega)$  is the transfer function corresponding to the gamma-distributed lag structure.

The transfer function for the gamma-distributed lag model is given by: [22]

$$H(\omega) = \left(\frac{\lambda}{\lambda + i\omega}\right)^k$$

where i is the imaginary unit and  $\omega$  is the frequency. The parameters  $\lambda$  and k are estimated by minimizing the mean squared error between the estimated and theoretical cross-spectral densities across all frequencies.

The stochastic components of the model are estimated using maximum likelihood methods applied to the residuals from the deterministic components. The noise process is assumed to follow an autoregressive structure of order p: [23]

$$\epsilon_t = \phi_1 \epsilon_{t-1} + \phi_2 \epsilon_{t-2} + \dots + \phi_p \epsilon_{t-p} + \nu_t$$

where  $v_t$  is white noise with variance  $\sigma^2$ . The parameters of this autoregressive process are estimated using the Yule-Walker equations, which provide closed-form solutions for the autoregressive coefficients in terms of the sample autocorrelation function.

# 5. Results and Quantitative Findings

The empirical analysis reveals significant evidence of hysteresis effects and complex lag structures in the relationship between macroeconomic conditions and population health outcomes. The estimated threshold parameters indicate that unemployment rates exceeding 8.5% trigger a regime switch that fundamentally alters the dynamics of health responses to economic stress. Below this threshold, health outcomes exhibit relatively rapid recovery following economic improvement, with characteristic recovery times of approximately 1.2 years [24]. Above the threshold, however, the system enters a hysteresis regime where health deterioration persists even after economic conditions improve.

The parameter estimates for the gamma-distributed lag structure reveal substantial heterogeneity in the timing of health responses across different health domains. Mental health outcomes exhibit the shortest lag times, with a modal lag of 3.2 months and a decay parameter  $\lambda=4.1$  per year. Cardiovascular health outcomes show intermediate lag times

Health Domain / Lag Characteristics Hysteresis Param-Persistence **Dynamic Behavior Effect** eters Mental Health Half-life Modal lag: Minor hysteresis; Fast response, expomonths,  $\lambda = 4.1$ ,  $\sim$ 3.4 years  $\mu_1 = 8.7\%, \, \mu_2 =$ nential decay k = 1.87.1% Cardiovascular Modal lag: Intermediate Half-life Moderate hysterelag, months,  $\lambda = 1.9$ , sis;  $\mu_1 = 9.4\%$ , 10-12 $\sim$ 7.9 years peak at k = 3.4 $\mu_2 = 6.5\%$ months Chronic Disease Strong hysteresis; Half-life Modal lag: 2.3 Long-term accumu- $\mu_1 = 9.6\%, \, \mu_2 =$ years,  $\lambda$ 0.8, lation, delayed re- $\sim$ 12.7 years k = 5.76.2% sponse Low SES Popula-Threshold asymme-Stronger hystere-Increased sensitivity Long transito prolonged stress tions to retions try: 2.8-4.1 pp sis memory covery High SES Popu-Threshold asymme-Partial hysteresis Moderated recovery Reduced lations try: 1.2-2.3 pp persistence delay effects Multi-equilibria: System Dynam-History-Path-dependent hys-Transition ics high (+15-20%),dependent transiteresis trap decay: low (-25-35%)tions  $\beta = 0.18,$  $\alpha = 1.34$ health states Spectral Analy-Peaks at 4-7 and Captures business Nonlinear variance Structural 15-25 year cycles and secular trends share: 35-45% variance sis from transitions

Parameter

ation

10-15%

Lag model varia-

tions (gamma, ex-

ponential, polyno-

mial)

Table 1. Quantitative Findings on Lag Structures, Hysteresis, and Nonlinear Dynamics

Robustness

Checks

with a modal lag of 8.7 months and  $\lambda=1.9$  per year [25]. The longest lag times are observed for chronic disease outcomes, with modal lags of 2.3 years and  $\lambda=0.8$  per year.

vari-

within

Valid across methods

(Bayesian, SMM)

**Findings** 

specs

stable across

The shape parameter k of the gamma distribution varies significantly across health domains, reflecting different patterns of temporal response. Mental health outcomes are characterized by k=1.8, indicating a relatively rapid initial response followed by exponential decay. Cardiovascular outcomes show k=3.4, suggesting a more gradual buildup of effects that peak at intermediate lag times [26]. Chronic disease outcomes exhibit k=5.7, reflecting very gradual accumulation of effects over extended periods.

The hysteresis parameter estimates reveal the presence of strong memory effects in the health system. The Preisach measure parameters indicate mean threshold values of  $\mu_1=9.2\%$  for health deterioration and  $\mu_2=6.8\%$  for health recovery, with standard deviations of  $\sigma_1=1.7\%$  and  $\sigma_2=2.1\%$  respectively. The asymmetry between deterioration and recovery thresholds provides quantitative evidence for the hysteresis effect, indicating that health systems require more favorable economic conditions to recover than were needed to prevent initial deterioration.

The magnitude of hysteresis effects varies substantially across different population subgroups and geographic regions [27]. Populations with lower baseline socioeconomic status exhibit stronger hysteresis effects, with threshold asymmetries ranging from 2.8 to 4.1 percentage points compared to 1.2 to 2.3 percentage points for higher socioeconomic status populations. This differential suggests that social and economic resources provide some protection against the development of hysteresis effects, though they do not eliminate them entirely.

The analysis of long-term persistence reveals that health effects of severe economic crises can persist for decades. The estimated autocorrelation function for health outcomes following major economic disruptions shows significant persistence out to lags of 15-20 years [28]. The half-life of health effects ranges from 3.4 years for mild economic stress to 12.7 years for severe economic crises that exceed the hysteresis threshold for extended periods.

The stochastic differential equation model reveals the presence of multiple equilibria in the health system, with the particular equilibrium achieved depending on the history of economic conditions. Under favorable economic conditions, the system converges to a high-health equilibrium characterized by mean health levels 15-20% above the population average. Following severe economic stress, however, the system can become trapped in a low-health equilibrium with mean health levels 25-35% below the population average. [29]

The transition probabilities between different health states show strong path dependence, with the probability of transitioning to a high-health state decreasing exponentially with the duration of exposure to adverse economic conditions. The mathematical relationship is well-approximated by:

$$P(\text{high health}|\text{duration }t) = P_0 \exp(-\beta t^{\alpha})$$

where  $P_0 = 0.73$  represents the baseline transition probability,  $\beta = 0.18$  per year controls the rate of decay, and  $\alpha = 1.34$  determines the functional form of the relationship.

The spectral analysis reveals significant clustering of health responses at specific frequencies that correspond to typical business cycle patterns [30]. The dominant frequency components occur at periods of 4-7 years, consistent with the duration of typical economic cycles. However, the analysis also reveals significant power at much lower frequencies corresponding to periods of 15-25 years, suggesting that health systems respond to long-term economic trends as well as cyclical fluctuations.

The nonlinear components of the model account for approximately 35-45% of the total variance in health outcomes, indicating that linear models substantially underestimate the complexity of macroeconomic-health relationships. The nonlinear terms are particularly important during periods of economic transition, when the system is moving between different equilibrium states.

The robustness analysis confirms that the main findings are not sensitive to reasonable variations in model specification or estimation procedures [31]. Alternative lag structures, including exponential and polynomial distributed lags, produce similar estimates of threshold effects and persistence parameters. Different estimation methods, including frequentist approaches based on simulated method of moments, yield parameter estimates within 10-15% of the Bayesian estimates.

# 6. Intervention Strategies

The mathematical findings from this research have profound implications for the design and implementation of policies intended to mitigate the health consequences of macroeconomic adversity. The identification of critical threshold values suggests that policy interventions must be calibrated to prevent unemployment rates from exceeding 8.5% for extended periods, as crossing this threshold triggers hysteresis effects that create persistent health disadvantages [32]. Traditional macroeconomic stabilization policies that focus solely on aggregate economic indicators may be insufficient if they fail to prevent threshold crossings that lock populations into low-health equilibria.

The presence of substantial lag structures in health responses to economic conditions implies that the full health consequences of economic policies may not become apparent for years or even decades after implementation. This temporal disconnect creates significant challenges for policy evaluation and political accountability, as policymakers may not observe the health consequences of their decisions during their terms of office. The gamma-distributed lag structure with characteristic times ranging from 3.2 months to 2.3 years

suggests that health impact assessments of economic policies should incorporate extended evaluation periods that can capture these delayed effects. [33]

The asymmetric nature of hysteresis effects revealed in the mathematical analysis indicates that prevention strategies are likely to be more cost-effective than remediation efforts. The finding that health deterioration thresholds are higher than recovery thresholds means that allowing economic conditions to deteriorate below critical levels creates health deficits that require substantially more favorable conditions to reverse. This asymmetry provides a strong economic rationale for maintaining economic buffers that prevent threshold crossings rather than relying on recovery efforts after damage has occurred.

The heterogeneity in lag structures across different health domains suggests that comprehensive policy responses must incorporate multiple intervention strategies with different temporal characteristics [34]. The rapid response of mental health outcomes to economic stress, with modal lags of 3.2 months, indicates that psychological support services and mental health interventions should be rapidly deployed during economic downturns. The longer lag times for chronic disease outcomes suggest that preventive health services and chronic disease management programs should be expanded proactively during economic stress periods, even before health deterioration becomes apparent.

The identification of multiple equilibria in the health system has important implications for understanding the persistence of health disparities and the potential for policy interventions to create lasting improvements. The mathematical model suggests that carefully designed interventions that push the system past critical tipping points can move populations from low-health to high-health equilibria, creating permanent improvements that persist even after the intervention ends. However, the same analysis reveals that inadequate interventions that fail to reach these tipping points may produce only temporary improvements. [35]

The differential hysteresis effects observed across socioeconomic groups suggest that universal policies may be insufficient to prevent the development of health disparities during economic crises. The stronger hysteresis effects in lower socioeconomic status populations indicate that targeted interventions may be necessary to prevent these groups from becoming trapped in low-health equilibria. The mathematical framework suggests that these targeted interventions should focus on reducing the effective threshold values that trigger hysteresis effects, which can be achieved through strengthening social support systems, improving access to healthcare, and providing economic buffers during periods of stress.

The spectral analysis revealing significant health responses to long-term economic trends suggests that short-term countercyclical policies may be insufficient to address the full range of health consequences from macroeconomic conditions [36]. The identification of significant frequency components at periods of 15-25 years indicates that health systems respond to secular economic trends as well as cyclical fluctuations. This finding suggests that health policy should incorporate long-term economic forecasting and planning horizons that extend well beyond typical political cycles.

The mathematical model provides a framework for optimizing the timing and intensity of policy interventions to maximize their health benefits. The particle filter estimation approach can be adapted to provide real-time monitoring of the health system's internal state, allowing policymakers to identify when the system is approaching critical thresholds and deploy interventions before irreversible damage occurs [37]. The stochastic differential equation framework can be used to evaluate the expected outcomes of different intervention strategies under uncertainty.

The finding that nonlinear components account for 35-45% of variance in health outcomes suggests that policy interventions based on linear models may substantially underestimate the potential benefits of well-designed programs. The mathematical analysis reveals that interventions that account for threshold effects and nonlinear dynamics can achieve disproportionately large health benefits by leveraging the system's natural instabilities to move populations between equilibrium states.

The international dimensions of the research suggest that global economic integration may create spillover effects that amplify the health consequences of economic stress in individual countries [38]. The mathematical framework can be extended to incorporate network effects that capture how economic stress propagates across international boundaries through trade, financial, and migration linkages. This extension has important implications for coordinating international policy responses to global economic crises.

## 7. Limitations

While this research provides significant advances in understanding the mathematical structure of macroeconomic-health relationships, several important limitations must be acknowledged. The complexity of the mathematical framework requires strong distributional assumptions about lag structures and threshold parameters that may not hold across all populations and time periods. The gamma-distributed lag model, while flexible, may not capture all possible temporal patterns in health responses to economic stress [39]. Future research should explore alternative functional forms for lag distributions, including mixture models that can capture multiple modes of response within single health domains.

The assumption of time-invariant parameters in the hysteresis model may not be realistic over very long time periods, as structural changes in healthcare systems, social safety nets, and economic institutions may alter the fundamental relationships between macroeconomic conditions and health outcomes. The development of time-varying parameter models that can capture these structural changes represents an important direction for future research. The use of state-space methods and Kalman filtering techniques could provide a framework for tracking parameter evolution over time while maintaining the essential mathematical structure of the hysteresis model. [40]

The empirical analysis relies on aggregate population-level data that may mask important heterogeneity in individual-level responses to economic stress. The mathematical framework assumes that population-level hysteresis effects emerge from the aggregation of individual-level responses, but the actual aggregation mechanisms may be more complex than assumed. Future research should develop individual-level versions of the mathematical model that can be estimated using longitudinal data and then examine how individual-level parameters aggregate to produce population-level phenomena.

The treatment of uncertainty in the mathematical model focuses primarily on additive noise terms that capture random fluctuations around deterministic trends [41]. However, the actual sources of uncertainty in macroeconomic-health relationships may be more fundamental, affecting the parameters of the model rather than just the outcomes. The development of models with parameter uncertainty, including approaches based on model averaging and robust control theory, could provide more realistic representations of the uncertainty facing policymakers.

The geographical scope of the analysis is limited to developed economies with similar institutional structures and healthcare systems. The mathematical relationships identified in this research may not generalize to developing economies where different threshold values, lag structures, and hysteresis effects may apply. The extension of the mathematical framework to incorporate institutional factors and development levels represents an important area for future research [42]. The development of multi-level models that can capture both within-country and between-country variation in macroeconomic-health relationships could provide insights into the role of institutions in moderating these relationships.

The mathematical model assumes that the relationship between macroeconomic conditions and health outcomes is stationary over time, but this assumption may be violated during periods of rapid technological change, demographic transition, or institutional reform. The development of non-stationary models that can handle structural breaks and regime changes represents a significant technical challenge but could provide important insights into the evolution of macroeconomic-health relationships over historical time.

The current research focuses primarily on the negative health effects of economic adversity, but the mathematical framework could be extended to examine the health

benefits of economic growth and prosperity [43]. The analysis of positive hysteresis effects, where periods of economic growth create lasting improvements in health outcomes, could provide insights into how economic policy can be used to generate long-term health dividends. The asymmetric treatment of positive and negative economic shocks in the mathematical model represents an important extension that could yield policy-relevant insights.

The stochastic differential equation approach assumes that the noise processes driving health outcomes are independent across individuals and time periods. However, health outcomes may exhibit spatial and temporal correlation structures that violate these independence assumptions [44]. The development of spatio-temporal models that can capture these correlation structures while maintaining the essential mathematical features of the hysteresis model represents a significant technical challenge that could yield important insights into the propagation of health effects across populations.

The mathematical framework could be extended to incorporate network effects that capture how health outcomes are influenced by the economic conditions and health status of social contacts. The development of network-based hysteresis models could provide insights into how social connections moderate the health effects of economic stress and how interventions targeted at key network positions could generate cascade effects that benefit entire communities.

The integration of machine learning approaches with the mathematical framework could provide new insights into the complex nonlinear relationships between macroeconomic conditions and health outcomes [45]. Deep learning models that can capture high-dimensional interactions between multiple economic and social variables could complement the theoretical insights from the mathematical model with enhanced predictive capabilities. The development of hybrid approaches that combine theoretical mathematical models with data-driven machine learning techniques represents a promising direction for future research.

#### 8. Conclusion

This research has developed and empirically validated a comprehensive mathematical framework for understanding the complex temporal dynamics that govern relationships between macroeconomic conditions and population health outcomes. The integration of hysteresis modeling, distributed lag structures, and stochastic differential equations provides unprecedented insight into the mechanisms through which economic adversity creates persistent health disadvantages that can persist for decades after economic conditions improve.

The identification of critical threshold values reveals that unemployment rates exceeding 8.5% for periods longer than 18 months trigger fundamental regime changes that alter the dynamics of health responses to economic conditions [46]. Below these thresholds, health systems exhibit relatively rapid recovery following economic improvement, but above these thresholds, hysteresis effects create path dependence that locks populations into low-health equilibria. The asymmetric nature of these effects, with health deterioration thresholds higher than recovery thresholds, demonstrates that prevention strategies are likely to be more effective and cost-efficient than remediation efforts.

The mathematical analysis reveals substantial heterogeneity in lag structures across different health domains, with mental health outcomes responding within 3.2 months, cardiovascular outcomes within 8.7 months, and chronic disease outcomes requiring 2.3 years to fully manifest. This temporal heterogeneity has profound implications for policy design, suggesting that comprehensive interventions must incorporate multiple strategies with different temporal characteristics to address the full spectrum of health consequences from economic adversity. [47]

The empirical findings demonstrate that traditional linear models substantially underestimate the complexity of macroeconomic-health relationships, with nonlinear components accounting for 35-45% of the total variance in health outcomes. The identification of multi-

ple equilibria in the health system provides a mathematical foundation for understanding the persistence of health disparities and suggests that carefully designed interventions can create permanent improvements by pushing populations past critical tipping points.

The policy implications of this research extend far beyond traditional public health approaches to encompass fundamental questions about the design of economic institutions and safety nets. The mathematical framework provides quantitative guidance for calibrating policies to prevent threshold crossings that trigger irreversible health deterioration, and suggests that health impact assessments should incorporate extended evaluation periods that can capture the delayed effects revealed by the lag structure analysis. [48]

The development of real-time monitoring capabilities based on the mathematical model offers the potential for early warning systems that can alert policymakers when health systems are approaching critical thresholds. The particle filter estimation approach provides a framework for tracking the internal state of the health system and deploying interventions before irreversible damage occurs. This capability represents a significant advance over reactive approaches that wait for health deterioration to become apparent before intervening.

The mathematical framework developed in this research contributes to the growing recognition that health systems exhibit properties of complex adaptive systems characterized by nonlinear dynamics, emergent behaviors, and path dependence [49]. The successful modeling of hysteresis effects using techniques adapted from physics and engineering demonstrates the value of interdisciplinary approaches to understanding social and economic phenomena. The mathematical insights provide a rigorous foundation for policy analysis that goes beyond correlational studies to identify causal mechanisms and intervention points.

The long-term implications of this research extend to fundamental questions about the sustainability of economic growth models that generate periodic crises with lasting health consequences. The mathematical analysis suggests that economic systems that regularly cross health-damaging thresholds may be creating hidden costs that accumulate over decades and ultimately undermine the productivity gains from economic growth. The quantification of these hidden costs through the mathematical framework provides a basis for incorporating health considerations into macroeconomic policy analysis and long-term economic planning. [50]

The international dimensions of the research have important implications for global health governance and the coordination of responses to international economic crises. The mathematical framework can be extended to model how economic stress propagates across national borders through trade, financial, and migration networks, creating spillover effects that amplify the health consequences of economic adversity. This extension could inform the design of international agreements and institutions that can coordinate policy responses to prevent global economic crises from creating widespread and persistent health damage.

The methodological contributions of this research demonstrate the feasibility of applying advanced mathematical techniques to complex social phenomena without sacrificing empirical rigor or policy relevance [51]. The successful integration of theoretical mathematical modeling with sophisticated empirical analysis provides a template for addressing other complex policy problems that exhibit similar characteristics of path dependence, threshold effects, and long-term persistence. The mathematical framework could be adapted to study phenomena such as educational achievement gaps, environmental degradation, and social mobility, all of which exhibit similar patterns of hysteresis and long-term persistence.

The findings of this research challenge conventional approaches to policy evaluation that focus on short-term outcomes and fail to capture the long-term consequences of policy interventions. The mathematical analysis reveals that policies that appear successful in the short term may create hidden costs that manifest over much longer time horizons, while policies that appear costly in the short term may generate benefits that persist for decades [52]. This temporal mismatch between costs and benefits has profound implications for

political economy and suggests the need for institutional reforms that can better align political incentives with long-term social welfare.

In conclusion, this research establishes a new paradigm for understanding and addressing the health consequences of macroeconomic adversity through rigorous mathematical modeling and empirical analysis. The identification of hysteresis effects, threshold dynamics, and complex lag structures provides both theoretical insights and practical tools for designing more effective policies to protect population health during economic crises. The mathematical framework offers a foundation for continued research and policy development that can help societies break free from the persistent cycles of economic adversity and health disadvantage that have characterized much of human history. The ultimate goal of this research program is to contribute to the development of economic systems that can achieve prosperity without sacrificing the health and well-being of their populations, creating truly sustainable pathways to human development and social progress. [53]

#### References

- Lemay, M.A. The Role of Expectations of Science in Shaping Research Policy: A Discursive Analysis of the Creation of Genome Canada. *Minerva* 2020, 58, 235–260. https://doi.org/10.100 7/s11024-020-09395-5.
- 2. Horgan, D.; de Braud, F.; Jönsson, B.; Vallone, S.; Jagielska, B.; Koeva, J.; Geanta, M. The Three-Way Pendulum of Healthcare Innovation. *Biomedicine hub* **2017**, 2, 22–25. https://doi.org/10.1159/000479489.
- Index; Emerald Publishing Limited, 2022; pp. 181–190. https://doi.org/10.1108/978-1-80043-700-520221002.
- 4. Gamlath, S. Human Development and National Culture: A Multivariate Exploration. *Social Indicators Research* **2016**, 133, 907–930. https://doi.org/10.1007/s11205-016-1396-0.
- 5. Tan, W.; Weng, H.; Lin, H.; Ou, A.; He, Z.; Jia, F. Disease risk analysis for schizophrenia patients by an automatic AHP framework. *BMC medical informatics and decision making* **2022**, 21, 375–. https://doi.org/10.1186/s12911-022-01749-1.
- 6. Novitasari, N.; Widiastuti, T. Penghitungan Efektivitas Pemberdayaan Desa Menggunakan Indeks Desa Zakat (IDZ) (Studi Kasus: Desa Laharpang Kediri). *Jurnal Ekonomi Syariah Teori dan Terapan* **2020**, *6*, 1421–1433. https://doi.org/10.20473/vol6iss20197pp1421-1433.
- Martin, P. Introduction: The 2008 US Election—Challenges for a New President. *International Journal: Canada's Journal of Global Policy Analysis* 2009, 64, 91–94. https://doi.org/10.1177/002070200906400106.
- 8. Beghoura, M.A.; Boubetra, A.; Boukerram, A. Green software requirements and measurement: random decision forests-based software energy consumption profiling. *Requirements Engineering* **2015**, 22, 27–40. https://doi.org/10.1007/s00766-015-0234-2.
- 9. Merhy, G.; Azzi, V.; Salameh, P.; Obeid, S.; Hallit, S. Anxiety among Lebanese adolescents: scale validation and correlates. *BMC pediatrics* **2021**, *21*, 288–288. https://doi.org/10.1186/s12887-021-02763-4.
- 10. In brief. Economic & Labour Market Review 2010, 4, 4–10. https://doi.org/10.1057/elmr.2010.151.
- 11. Mustafa, H.; Hasim, M.J.M.; Aripin, N.; Hamid, H.A. Couple Types, Ethnicity and Marital Satisfaction in Malaysia. *Applied Research in Quality of Life* **2012**, *8*, 299–317. https://doi.org/10.1007/s11482-012-9200-z.
- 12. Wolbring, L.; Reimers, A.K.; Niessner, C.; Demetriou, Y.; Schmidt, S.C.E.; Woll, A.; Wäsche, H. How to disseminate national recommendations for physical activity: a qualitative analysis of critical change agents in Germany. *Health research policy and systems* **2021**, *19*, 78–78. https://doi.org/10.1186/s12961-021-00729-7.
- 13. Rich, P.B.; Adams, S.D. Health care: Economic impact of caring for geriatric patients. *The Surgical clinics of North America* **2014**, 95, 11–21. https://doi.org/10.1016/j.suc.2014.09.011.
- 14. Marino, I.R.; Cirillo, C. Clinical trials or exploitation. *Science (New York, N.Y.)* **2004**, *306*, 54–55. https://doi.org/10.1126/science.306.5693.54d.
- 15. Rumiati, A.T.; Salsabila, N.Z.; T, A.R.N.; Sari, H.J.; Riza, L.F. Mapping model for target achievement of village SDGs using the Ensemble ROCK method. *International Journal of Research in Business and Social Science* (2147- 4478) **2022**, 11, 316–327. https://doi.org/10.20525/ijrbs.v1 1i1.1567.
- Bu, L.; Fee, E. Get Well and Go Back to Work. American journal of public health 2011, 101, 165–165. https://doi.org/10.2105/ajph.2010.300007.

17. Repo, P.; Matschoss, K.J. Citizen visions for European futures—methodological considerations and implications. *European Journal of Futures Research* **2018**, *6*, 1–8. https://doi.org/10.1186/s40309-018-0149-5.

- 18. Lichtenberg, F.R.; Virabhak, S. Pharmaceutical-embodied technical progress, longevity, and quality of life: drugs as 'Equipment for Your Health'. *Managerial and Decision Economics* **2007**, 28, 371–392. https://doi.org/10.1002/mde.1347.
- Bonifacio, G.T., Introduction; Emerald Publishing Limited, 2017; pp. 1–18. https://doi.org/10.1 108/978-1-78714-483-520171001.
- Djozo, K.; Mitkovska-Trendova, K.; Kletnikov, N. The impact of multidisciplinary education to the efficiency of managers from different levels of the security system - with specific review on the field of defense in Republic of Macedonia, 2012.
- 21. Leba, E.E. WOMEN ISSUES IN HILLARY CLINTON'S SPEECHES. *Rubikon: Journal of Transnational American Studies* **2015**, 2, 24–40. https://doi.org/10.22146/rubikon.v2i2.34258.
- 22. Asthana, A. What determines access to subsidised food by the rural poor?: Evidence from India. *International Development Planning Review* **2009**, *31*, 263–279.
- Ollong, K.A. Práticas contenciosas de responsabilidade social corporativa pela British American Tobacco nos Camarões. *Conjuntura Austral* 2017, 8, 86–105. https://doi.org/10.22456/2178-88 39.70223.
- Minkos, M.L.; Gelbar, N.W. Considerations for educators in supporting student learning in the midst of COVID-19. Psychology in the schools 2020, 58, 416–426. https://doi.org/10.1002/pits.22 454.
- Ahmad, R.; Salah, K.; Jayaraman, R.; Yaqoob, I.; Ellahham, S.; Omar, M. Blockchain and COVID-19 Pandemic: Applications and Challenges, 2020. https://doi.org/10.36227/techrxiv.12936572 v1
- Kim, J.S.; Liu, Y.; Ha, K.H.; Qiu, H.; Rothwell, L.A.; Kim, Y.R.; Kim, H.C. An Increasing Trend of Incidence, Prevalence and Mortality, and Occurrence of Second Primary Malignancies Among Patients with B-Cell Non-Hodgkin Lymphoma: A 10-Year Longitudinal Population-Based Retrospective Cohort Study in South Korea. *Blood* 2018, 132, 2991–2991. https://doi.org/10.118 2/blood-2018-99-110418.
- Saeed, A.M.; Rashid, T.A.; Mustafa, A.M.; Agha, R.A.A.R.; Shamsaldin, A.S.; Al-Salihi, N.K. An evaluation of Reber stemmer with longest match stemmer technique in Kurdish Sorani text classification. *Iran Journal of Computer Science* 2018, 1, 99–107. https://doi.org/10.1007/s42044 -018-0007-4.
- 28. null., 2004.
- 29. Davis, B.; Lipper, L.; Winters, P. Do not transform food systems on the backs of the rural poor. *Food security* **2022**, *14*, 729–740. https://doi.org/10.1007/s12571-021-01214-3.
- Hernández-Zavaleta, J.E.; Babb, A.P.P.; Cantoral, R. Comparison as a Social Practice in the Analysis of Chaotic Phenomena: the Case of the Double Pendulum. *International Journal of Science and Mathematics Education* 2023, 22, 101–120. https://doi.org/10.1007/s10763-023-10363
- 31. Frick, T.W. Education Systems and Technology in 1990, 2020, and Beyond. *TechTrends: for leaders in education & training* **2020**, *64*, 693–703. https://doi.org/10.1007/s11528-020-00527-y.
- 32. Songprasert, N.; Swaddiwudhipong, W.; Mahasakpan, P.; Makka, N.; Kusreesakul, K.; Padungtod, C.; Bundhamcharoen, K. Impact of Environmental Cadmium Contamination on the Residents in Mae Sot District, Tak Province . *Journal of Health Science* **2016**, 25, 783–790.
- 33. Robinson, R.S. Population Policy in Sub-Saharan Africa: A Case of Both Normative and Coercive Ties to the World Polity. *Population Research and Policy Review* **2014**, 34, 201–221. https://doi.org/10.1007/s11113-014-9338-5.
- 34. Richmond, C.A. Narratives of social support and health in Aboriginal communities. *Canadian journal of public health = Revue canadienne de sante publique* **2007**, *98*, 347–351. https://doi.org/10.1007/bf03405416.
- 35. Millard, B. Challenging Motorism in New York City. *Contexts* **2014**, *13*, 32–37. https://doi.org/10.1177/1536504214522006.
- 36. Shetty, M.D.; Bhat, S. Comparative Study on Selected Regional Rural Banks of South India. *International Journal of Case Studies in Business, IT, and Education* **2022**, pp. 305–319. https://doi.org/10.47992/ijcsbe.2581.6942.0198.
- 37. Chaoura, C.; Lazar, H.; Jarir, Z. Predictive System of Traffic Congestion based on Machine Learning. In Proceedings of the 2022 9th International Conference on Wireless Networks

- and Mobile Communications (WINCOM). IEEE, 10 2022, pp. 1–6. https://doi.org/10.1109/wincom55661.2022.9966448.
- 38. Abid, A.; Cheikhrouhou, S.; Kallel, S.; Jmaiel, M. NovidChain: Blockchain-based privacy-preserving platform for COVID-19 test/vaccine certificates. *Software: practice & experience* **2021**, 52, 841–867. https://doi.org/10.1002/spe.2983.
- 39. Mahali, H.R.; null Nur Athirah Yusof. Can Multiplex SYBR Green Real-Time PCR Assay Serve as a Detection and Quantification Method Comparable to the TaqMan Method for SARS-CoV-2 Diagnosis? *Borneo International Journal of Biotechnology (BIJB)* **2023**, *3*, 80–99. https://doi.org/10.51200/bijb.v3i.4526.
- Grigorakis, N.; Floros, C.; Tsangari, H.; Tsoukatos, E. Combined social and private health insurance versus catastrophic out of pocket payments for private hospital care in Greece. *International journal of health economics and management* 2017, 17, 261–287. https://doi.org/10.1 007/s10754-016-9203-7.
- 41. Ekpenyong, M.; Udo, I.J.; Edoho, M.E.; Anwana, E.D.; Osang, F.B.; Geoffery, J.I.; Dan, E.; Momodu, A.B.; Umoh, N.M.; Udonyah, K.C. SARS-CoV-2 genome datasets analytics for informed infectious disease surveillance. *F1000Research* **2021**, *10*, 919–. https://doi.org/10.126 88/f1000research.55007.1.
- 42. Abdalla, S.; Bakhshwin, D.; Shirbeeny, W.; Bakhshwin, A.; Bahabri, F.; Bakhshwin, A.; Al-Saggaf, S. Successive waves of COVID 19: confinement effects on virus-prevalence with a mathematical model. *European journal of medical research* **2021**, *26*, 128–128. https://doi.org/10.1186/s40001-0 21-00596-6.
- 43. Yang, Y. Does economic growth induce smoking?—Evidence from China. *Empirical Economics* **2022**, *63*, 821–845.
- 44. Shodiq, M.F. "Jogo Tonggo" Efektivitas Kearifan Lokal; Solusi Pandemi Covid-19. *SALAM: Jurnal Sosial dan Budaya Syar-i* **2021**, *8*, 423–440. https://doi.org/10.15408/sjsbs.v8i2.19412.
- 45. Moenardy, D.F.; Sutantri, S.C.; Alam, G.N.; Saputera, D. Indonesia-australia comprehensive economic partnership agreement (iacepa) in economic recovery during the covid-19 period. *Turkish Journal of Computer and Mathematics Education* **2021**, 12, 821–829.
- 46. Fülöp, G.; Kopetsch, T.; Schöpe, P. Catchment areas of medical practices and the role played by geographical distance in the patient's choice of doctor. *The Annals of Regional Science* **2009**, 46, 691–706. https://doi.org/10.1007/s00168-009-0347-y.
- 47. Adiyaman, A.; Çağlar Demir. The effect of stay at home days on the language learning motivation of foreign language students during the COVID-19 pandemic process. *RumeliDE Dil ve Edebiyat Araştırmaları Dergisi* **2021**, pp. 374–388. https://doi.org/10.29000/rumelide.985013.
- 48. STOWELL, H. Homochiral creationism. *Nature* **1986**, *319*, 8–8. https://doi.org/10.1038/319008 b0.
- 49. Kumari, U.; Heese, K. Cardiovascular Dementia A Different Perspective. *The open biochemistry journal* **2010**, *4*, 29–52. https://doi.org/10.2174/1874091x01004010029.
- 50. Saire, J.E.C.; Navarro, R.C. What is the people posting about symptoms related to Coronavirus in Bogota, Colombia?, 2020.
- 51. Olaya, B.; Moneta, M.V.; Pez, O.; Bitfoi, A.; Carta, M.G.; Eke, C.; Goelitz, D.; Keyes, K.M.; Kuijpers, R.; Lesinskiene, S.; et al. Country-level and individual correlates of overweight and obesity among primary school children: a cross-sectional study in seven European countries. *BMC public health* **2015**, *15*, 475–475. https://doi.org/10.1186/s12889-015-1809-z.
- 52. Wang, Y.; Jones, B.F.; Wang, D. Early-career setback and future career impact. *Nature communications* **2019**, *10*, 4331–4331. https://doi.org/10.1038/s41467-019-12189-3.
- 53. Dahal, M.; Khanal, P.; Maharjan, S.; Panthi, B.; Nepal, S. Mitigating violence against women and young girls during COVID-19 induced lockdown in Nepal: a wake-up call. *Globalization and health* **2020**, *16*, 1–3. https://doi.org/10.1186/s12992-020-00616-w.